



# Comparison of Forward Operators for Polarimetric Radars Aiming for Data Assimilation



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# Forward Operators for Polarimetric Radars

(1) WRF

## Two-moment microphysical scheme

(Morrison and Gettleman J. Climate 2002)

$$\phi(D) = N_0 D^\mu e^{-\Lambda D}$$

$N_0$  Intercept parameter

$\Lambda$  Slope parameter

$\mu$  Spectral shape parameter

Predict

Prognostic equations for number  $N$  and mass concentration  $q$  of hydrometeors

(2) Two types of variable converters

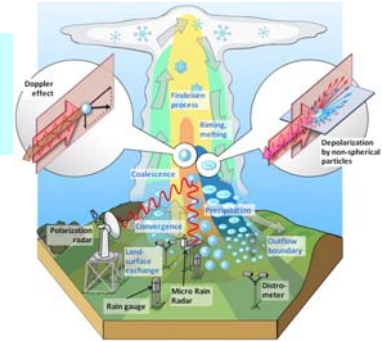
### Model variables -> pol. observation

- T-matrix (Mishchenko 2000)
- Fitting of scattering amplitude (Zhang et al. 2001)

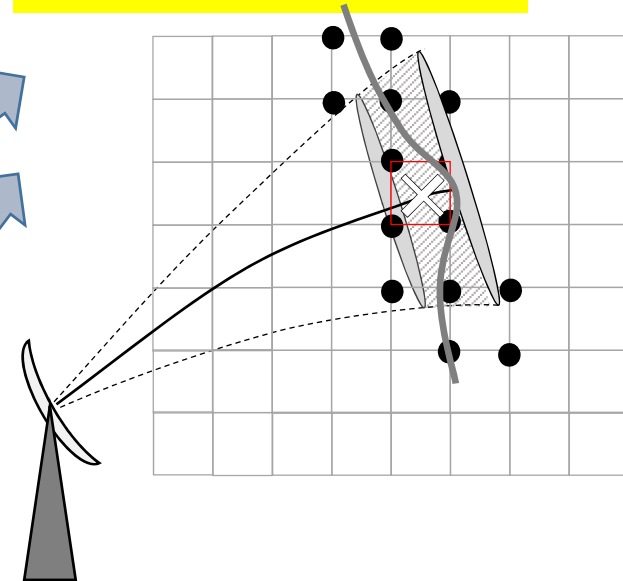
### Pol. observation -> model variable

- $Q_r - (Z_h, Z_{dr})$
- $Q_r - (K_{dp}, Z_{dr})$
- $Q_r - (K_{dp})$

(Bringi and Chandrasekar 2001)



(3) Space interpolator



- Beam broadening with Gaussian weights in both horizontal and vertical directions
- Consider the bending effect

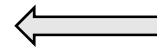
# Variable converters (1) (model to observation)

Oblateness (Brandes et al. 2005)

From spherical rain in the model to spheroid

$$r = 0.9951 + 2.51 \times 10^{-2}D - 3.644 \times 10^{-2}D^2 + 5.303 \times 10^{-3}D^3 - 2.492 \times 10^{-4}D^4$$

T-matrix (direct scattering calculation)



TMX

Drop size **D** and **number** of rainwater are provided by the model.

(Doviak and Zrnica 1993, Smyth and Illingworth 1998, Oguchi 1973)

Observation

$$Z_{H,V} = \left( \frac{4\lambda^4}{\pi^4 |K_w|^2} \right) \int_{r_2}^{r_1} |S_{h,v}(D)|^2 n(D) dD$$

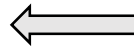
$$K_{DP} = \frac{2 \times 180 \times 10^{-3} \lambda}{\pi} \int_{r_1}^{r_2} \text{Re}[S_h(D) - S_v(D)] n(D) dD$$

$$A_H = 8.686 \times 10^{-3} \lambda \int_{r_1}^{r_2} \text{Im}[S_h(D)] n(D) dD$$

$$A_{DP} = 8.686 \times 10^{-3} \lambda \int_{r_1}^{r_2} \text{Im}[S_h(D) - S_v(D)] n(D) dD$$

The most accurate operator in theory, but not differential (not available for variational DA)

Fitting (indirect scattering calculation)



(Zhang et al. 2001)

$$|S_{h,v}(D)| = \alpha_{h,v} D^{\beta_{h,v}}$$

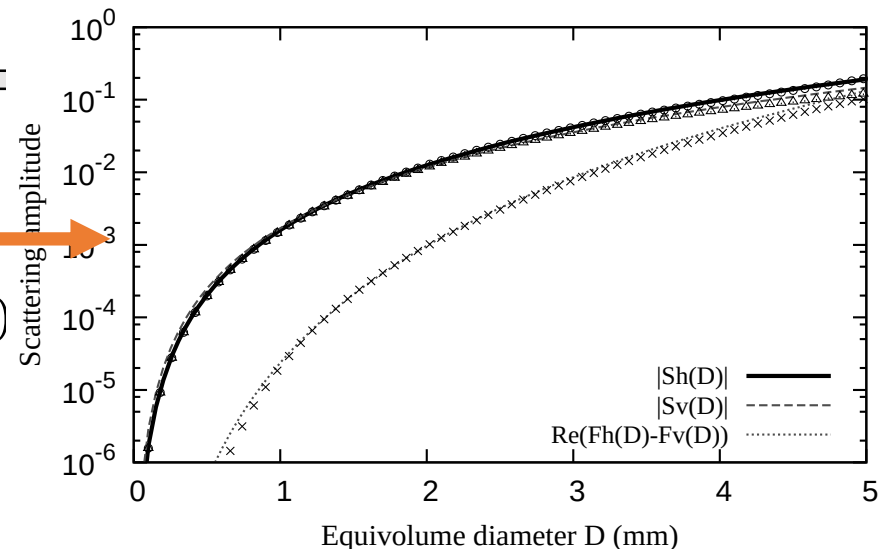
$$Z_{H,V} = \frac{4\lambda^4}{\pi^4 |K_w|^2} \left( \alpha_{h,v}^2 N_0 \Lambda^{-(2\beta_{h,v}+1)} \Gamma(2\beta_{h,v} + 1) \right)$$

$$K_{DP} = \frac{180\lambda}{\pi} N_0 \alpha_k \Lambda^{-(\beta_k+1)} \Gamma(\beta_k + 1)$$

$$A_H = \alpha_H K_{DP}^{\beta_H}$$

$$A_{DP} = \alpha_d K_{DP}^{\beta_d}$$

$\alpha, \beta$  are fitting coefficients.



# Variable converters (2)

## (observation to model)

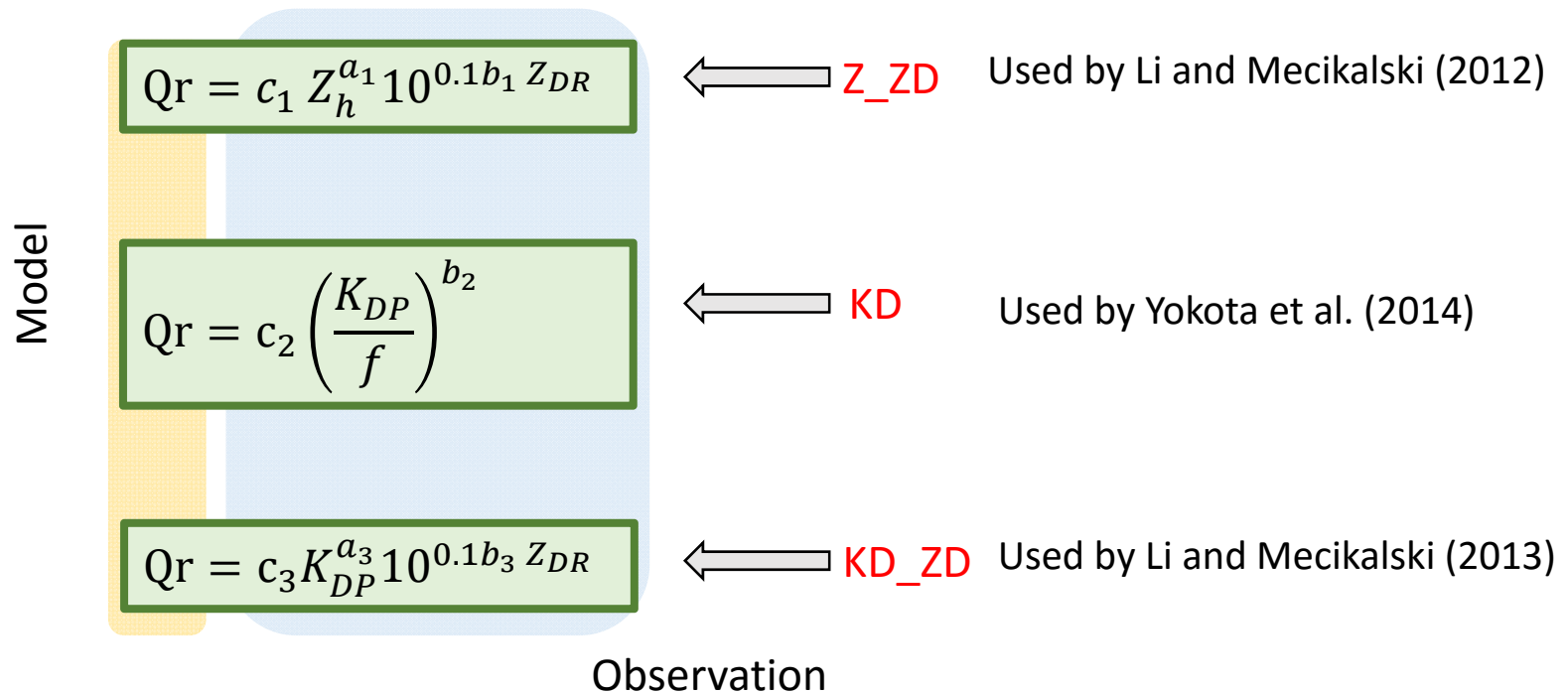
$Z_h$ ,  $Z_{DR}$  and  $K_{DP}$  are  
observed by  
polarimetric radars

### Physically based methods

Derived theoretically or fitting with scattering calculation

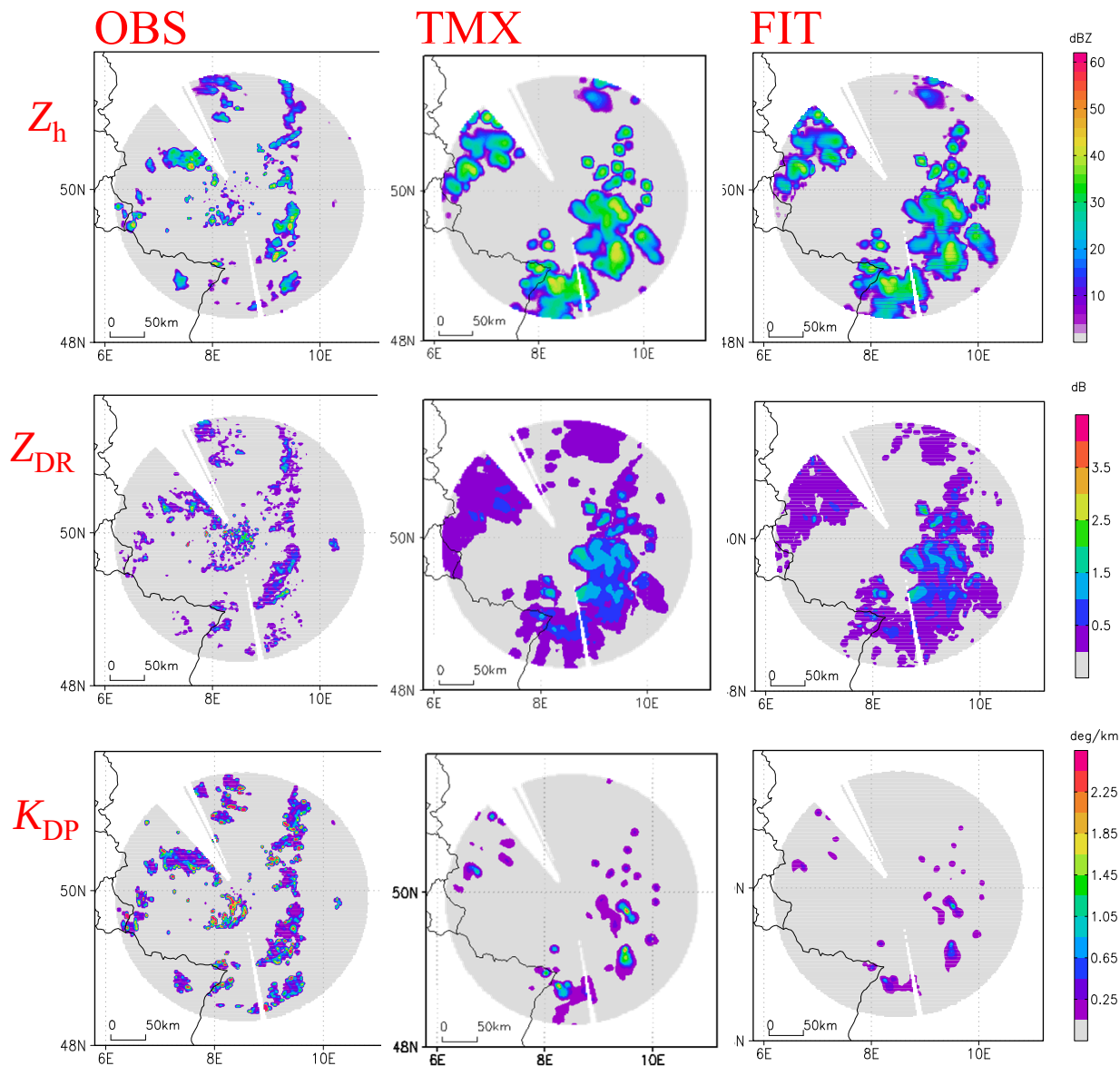
Suggested by radar meteorologists

(Bringi and Chandrasekar 2001)



$a_x, b_x, c_x$  are constants

# Horizontal distributions of Pol. parameters (model to obs)



- TMX and FIT captured sporadic clouds with their locations and intensities well.
- $Z_h$  and  $Z_{DR}$  with TMX and FIT distribute more widely than OBS.
- Observed  $K_{DP}$  shows stronger values.

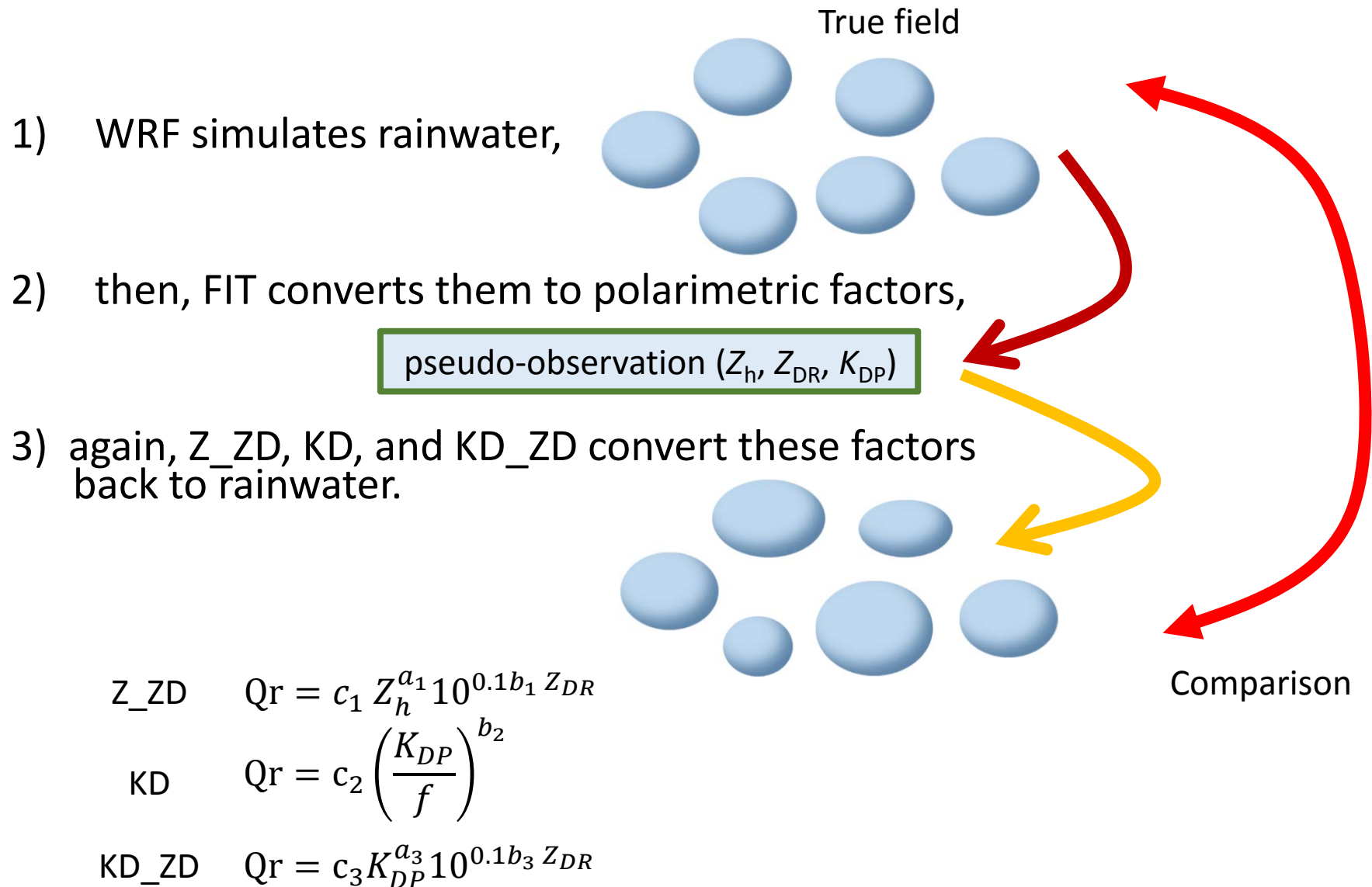
## Statistics (model to obs)

|           | $Z_h$ (dBZ) |       | $Z_{DR}$ (dB) |      | $K_{DP}$ ( $^{\circ}$ km $^{-1}$ ) |      |
|-----------|-------------|-------|---------------|------|------------------------------------|------|
|           | AVG         | STD   | AVG           | STD  | AVG                                | STD  |
| OBS       | 18.99       | 11.10 | 0.93          | 1.05 | 1.31                               | 1.54 |
| TMX       | 20.40       | 10.92 | 0.60          | 0.37 | 0.25                               | 0.36 |
| FIT       | 19.23       | 10.37 | 0.55          | 0.41 | 0.25                               | 0.18 |
| TMX - OBS | 1.05        | 15.04 | -0.26         | 0.96 | -0.76                              | 1.53 |
| FIT - OBS | -0.10       | 14.68 | -0.30         | 0.99 | -0.91                              | 1.47 |

- Regarding  $Z_h$ , FIT is slightly closer to OBS than TMX.
- In  $Z_{DR}$ , both converters look similar.
- $K_{DP}$  of OBS looks strange compared with TMX and FIT.

FIT is mostly the same with TMX, but slightly better

# FIT is used as a pseudo-observation generator

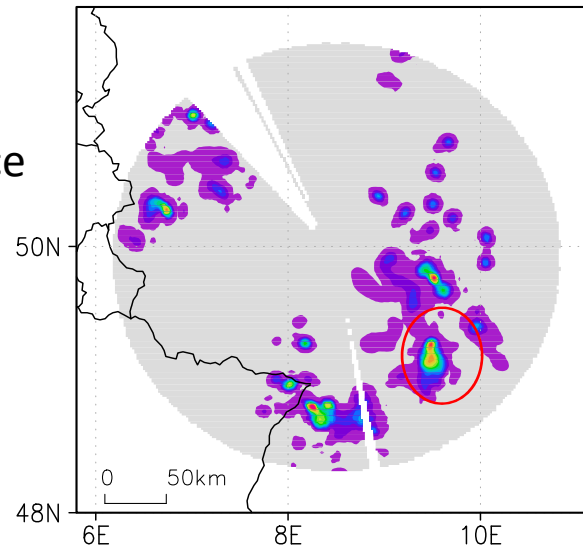




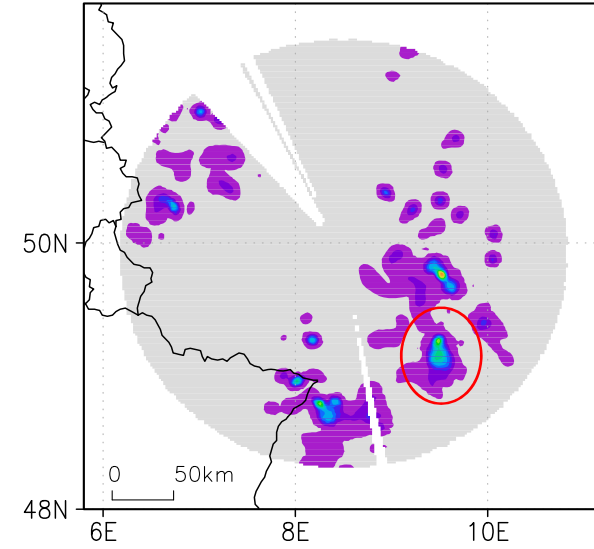
# Rainwater content (obs to model)

- KD looks mostly fair.
- Z\_ZD and KD\_ZD produce stronger intensities.

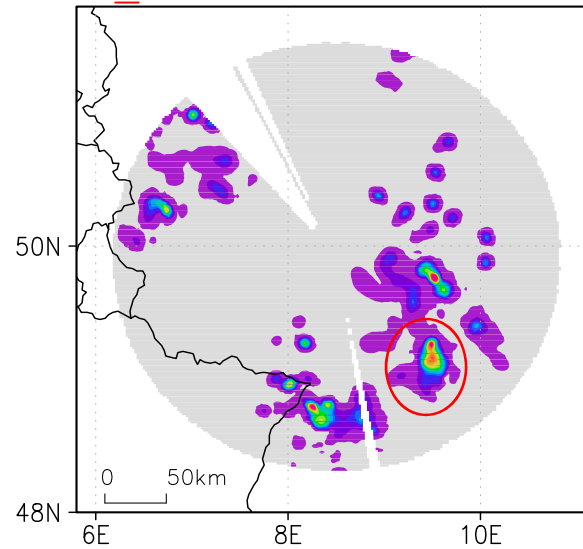
**Z\_ZD**



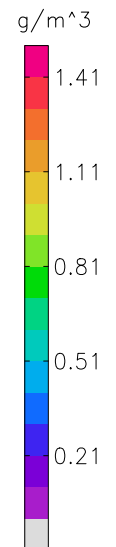
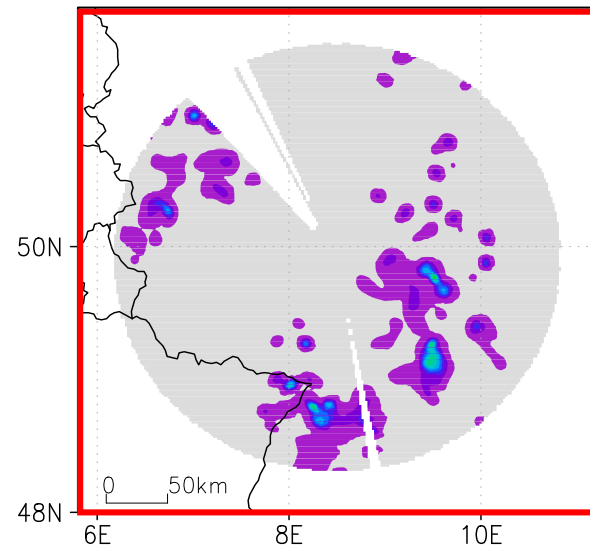
**KD**



**KD\_ZD**



**TRUE**





## Statistics (obs to model)

|       |      |      | Difference from True |      |
|-------|------|------|----------------------|------|
|       | AVG  | STD  | AVG                  | STD  |
| True  | 0.08 | 0.12 | —                    | —    |
| Z_ZD  | 0.11 | 0.18 | -0.033               | 0.07 |
| KD    | 0.07 | 0.12 | 0.006                | 0.03 |
| KD_ZD | 0.12 | 0.22 | 0.044                | 0.10 |

- Average and STD in KD show good agreement with True.
- KD has the smallest bias and STD against True.

KD is the best.

# Attenuation effect (obs to model)

## Super cell case

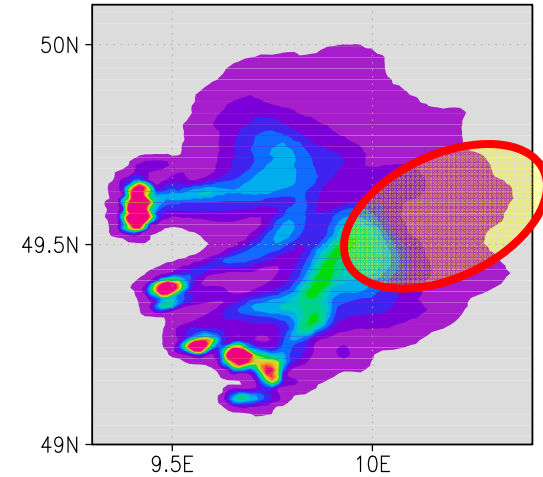
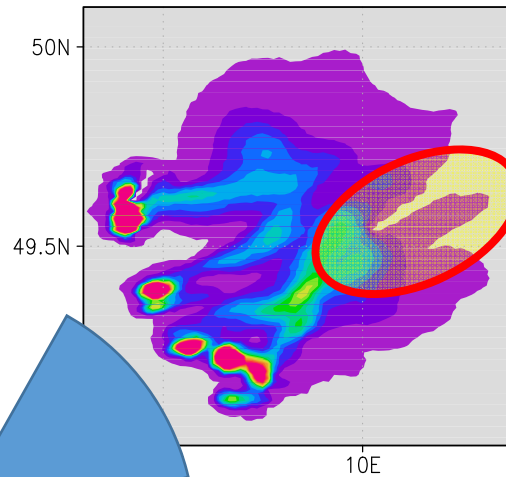
Since  $Z_h$  and  $Z_{DR}$  are affected by  $A_h$  and  $A_{DP}$ , respectively, only KD is not affected by the attenuation.

A virtual radar is located at beyond the left-bottom corner.



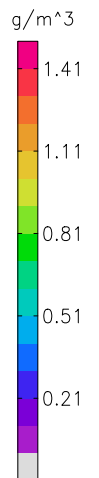
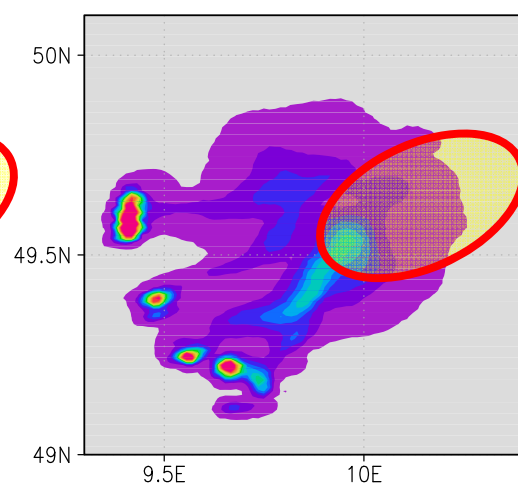
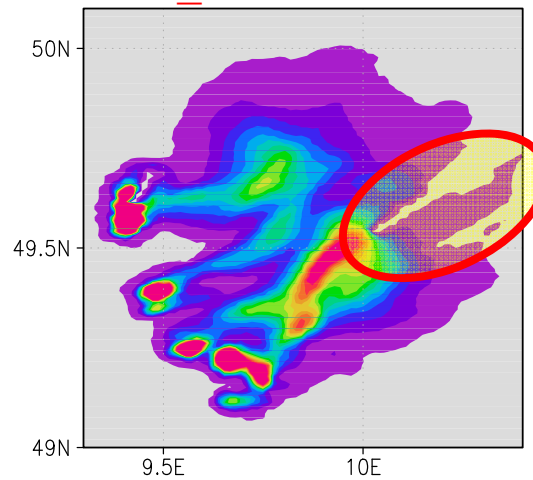
$Z\_ZD$

KD



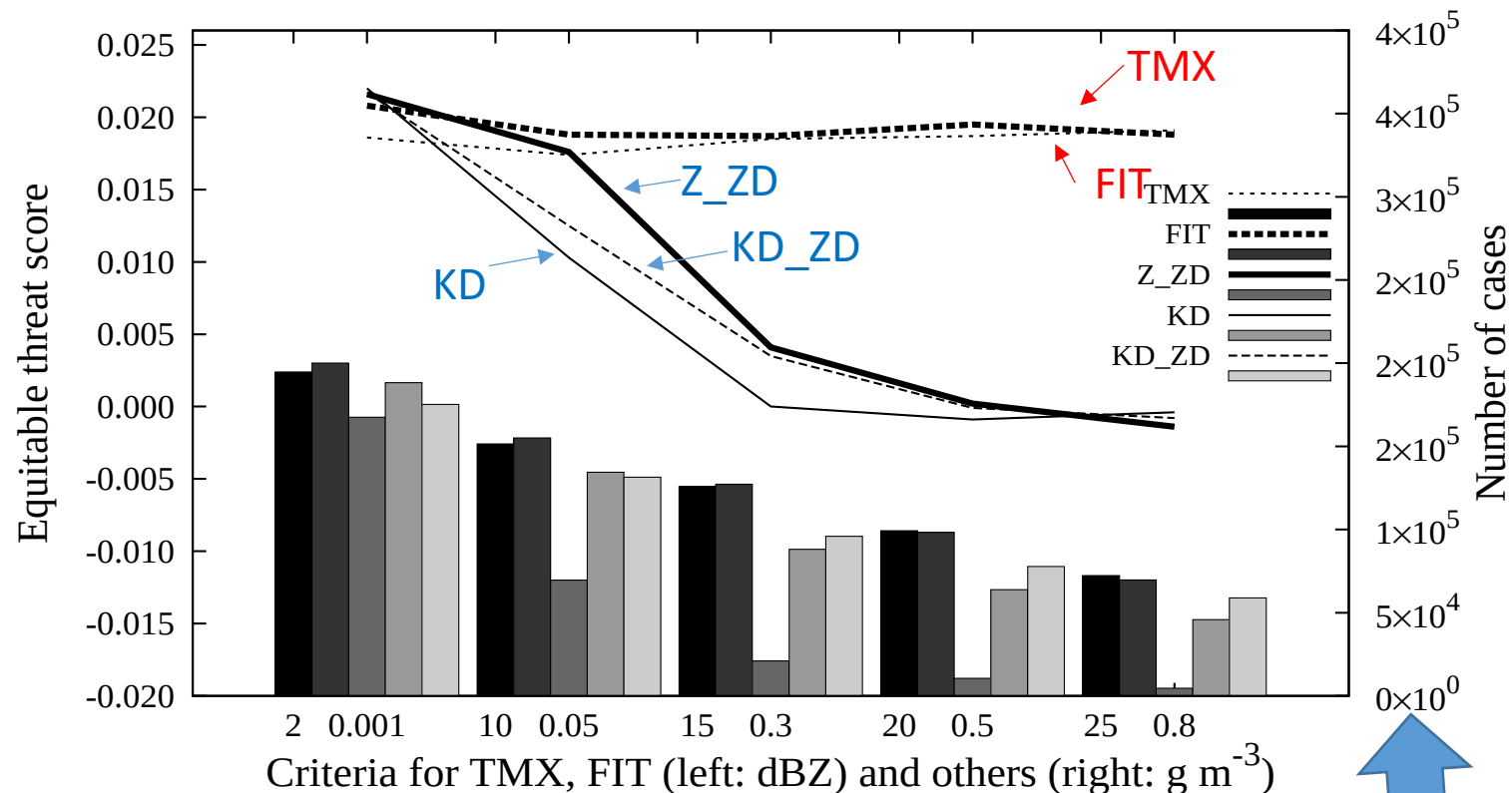
KD\_ZD

TRUE



KD is the best

# Equitable threat scores against observation comparison of (model to obs) and (obs to model)



- TMX and FIT are evaluated in dBZ, while Z\_ZD, KD, and KD\_ZD are in  $\text{g m}^{-3}$ . Since it is hard to compare factors in different units each other, we carefully chose criteria to capture similar numbers.
- TMX and FIT look better than other converters, but values of the threat scores are quite low.

Numbers of samples  
of each bin

# Conclusions of the comparison

- FIT is close to TMX, but slightly better.
- KD is the best in Z\_ZD, KD, and KD\_ZD.  
← KD\_ZD and Z\_ZD are affected by the attenuation.
- (model to obs) type converters are better than (obs to model) type.  
however, since threat scores are quite low, we need further examinations through DA.