

# Data assimilation for local rainfall near Tokyo on 18 July 2013 using EnVAR with observation space localization

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# What is EnVAR?

## Data Assimilation

Analysis  $\mathbf{x}_0$  is provided from First guess  $\mathbf{x}_0^f$  and Observation  $\mathbf{y}_t$ .

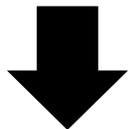
$\mathbf{x}_0$  takes a maximum likelihood value when cost function  $J$  is minimum ( $\nabla J=0$ ).

Cost  
Function

$$J = \underbrace{\frac{1}{2} (\mathbf{x}_0 - \mathbf{x}_0^f)^T \mathbf{B}^{-1} (\mathbf{x}_0 - \mathbf{x}_0^f)}_{\text{Background term}} + \underbrace{\frac{1}{2} \sum_t [H(M_t(\mathbf{x}_0)) - \mathbf{y}_t]^T \mathbf{R}_t^{-1} [H(M_t(\mathbf{x}_0)) - \mathbf{y}_t]}_{\text{Observation term}}$$

Gradient

$$\nabla J \equiv \frac{\partial J}{\partial \mathbf{x}_0} = \mathbf{B}^{-1} (\mathbf{x}_0 - \mathbf{x}_0^f) + \sum_t \left[ \frac{\partial H(M_t(\mathbf{x}_0))}{\partial \mathbf{x}_0} \right]^T \mathbf{R}_t^{-1} [H(M_t(\mathbf{x}_0)) - \mathbf{y}_t]$$



Several methods are classified using how to solve  $\nabla J=0$ .

Method	Background covariance	How to solve $\mathbf{x}_0$	How to calculate <span style="background-color: yellow;"> </span>
3DVAR,4DVAR	Statistic	Implicitly	With adjoint of M and H
Hybrid-4DVAR	Ensemble-based	Implicitly	With adjoint of M and H
EnKF (LETKF)	Ensemble-based	<b>Explicitly</b>	Ensemble approximation
EnVAR	Ensemble-based	<b>Implicitly</b>	Ensemble approximation

**EnVAR provides analysis implicitly without adjoint models**

# EnVAR with observation space localization

**Analysis**

$$\overline{\mathbf{x}}_t^a = \overline{\mathbf{x}}_t^f + \sum_j \delta \mathbf{x}_{t,j}^f \circ \mathbf{w}_j$$

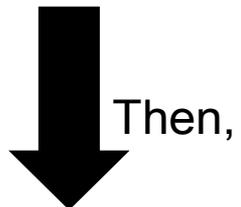
**Background error covariance**

$$\mathbf{B} = \frac{1}{M-1} \mathbf{L} \circ \sum_j \delta \mathbf{x}_{0,j}^f \delta \mathbf{x}_{0,j}^{f T}$$

i: analysis points  
k: observation points  
t: time slots  
j: ensemble members

Analysis valuable is transformed from  $\mathbf{x}$  to  $\mathbf{w}$

Localization factor



**Gradient of J**

$$\frac{\partial J}{\partial \mathbf{w}_{ij}} = (M-1) \mathbf{w}_{ij} + \sum_{k,t} L_{ik} \delta H_{kj,t} R_{k,t}^{-1} \left[ H_k \left( \overline{\mathbf{x}}_t^a \right) - y_{k,t} \right]$$

Perturbation of H

Observation error variance

Observation operator (non-linear)

- Localization factor in observation term
- Equivalent to B-localization
- Globally defined J

Similar to LETKF

Different from LETKF

# Observation system simulation experiments with SPEEDY model

Number of members: 20

Assimilation window: 6 hours

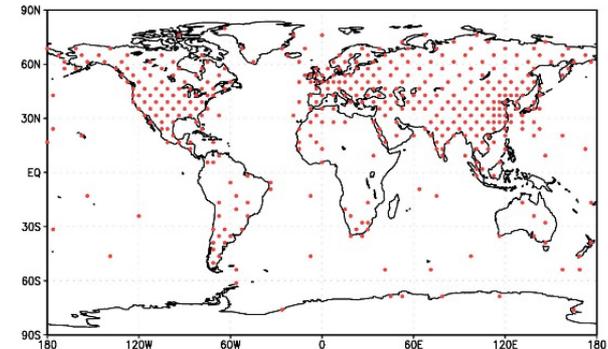
Localization radius:  $\sigma_H=1000(\text{km})$ ,  $\sigma_V=0.1(\text{sigma})$

Observations: **U, V, T, RH, Ps**

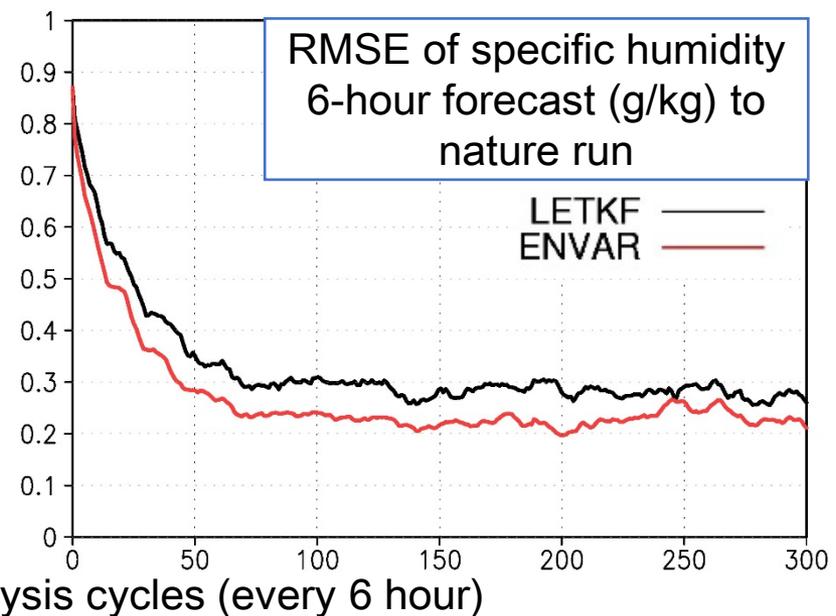
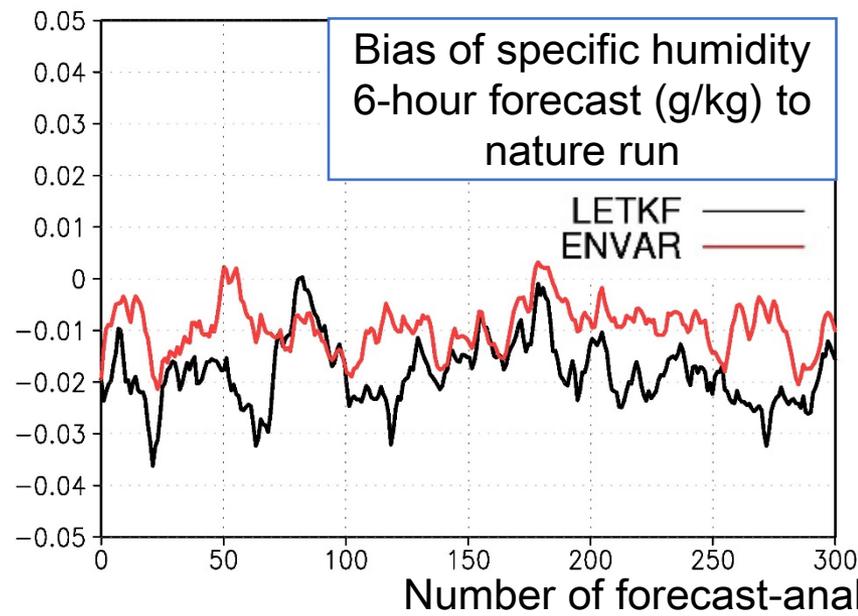
Inflation: Multiplicative (=1.1)

Analysis time: Center of the window (t=3h)

Observation time: t=1h, 3h, 5h



Positions of observations



**Is EnVAR better than LETKF in real obs. data assimilation?**

# Local Rainfall on 18 July 2013

15–16JST

16–17JST

17–18JST

18–19JST

19–20JST

20–21JST

RAIN(mm/1hr) 201307180700

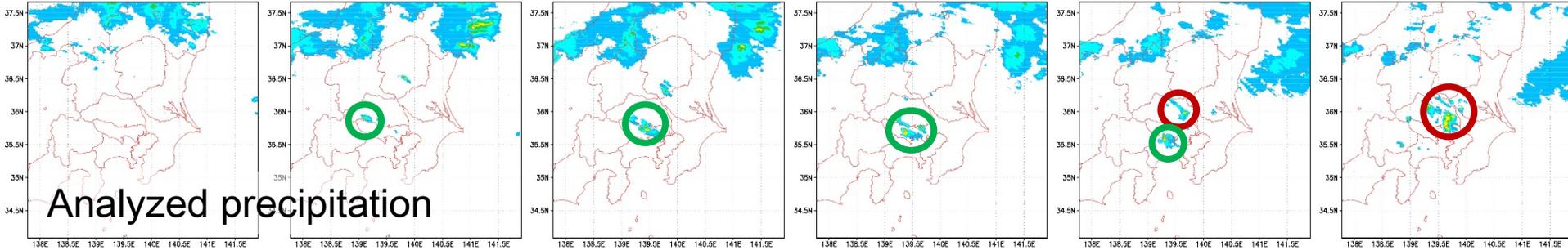
RAIN(mm/1hr) 201307180800

RAIN(mm/1hr) 201307180900

RAIN(mm/1hr) 201307181000

RAIN(mm/1hr) 201307181100

RAIN(mm/1hr) 201307181200



RAIN(mm/1hr) 201307180700

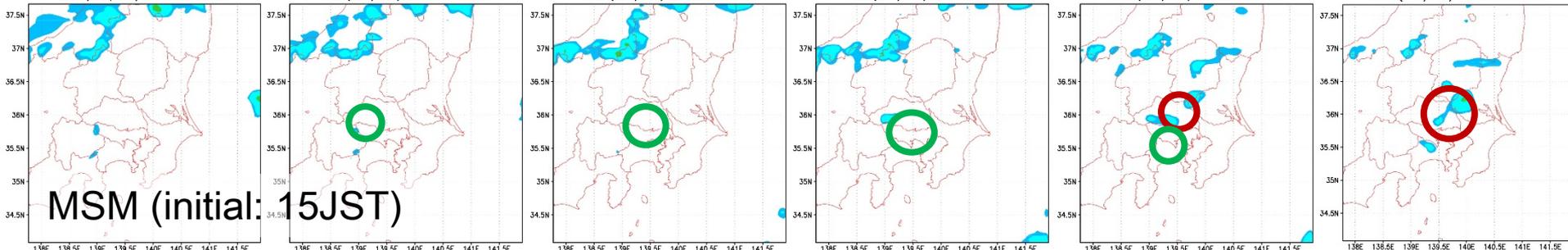
RAIN(mm/1hr) 201307180800

RAIN(mm/1hr) 201307180900

RAIN(mm/1hr) 201307181000

RAIN(mm/1hr) 201307181100

RAIN(mm/1hr) 201307181200



0.4 1 5 10 20 50 100

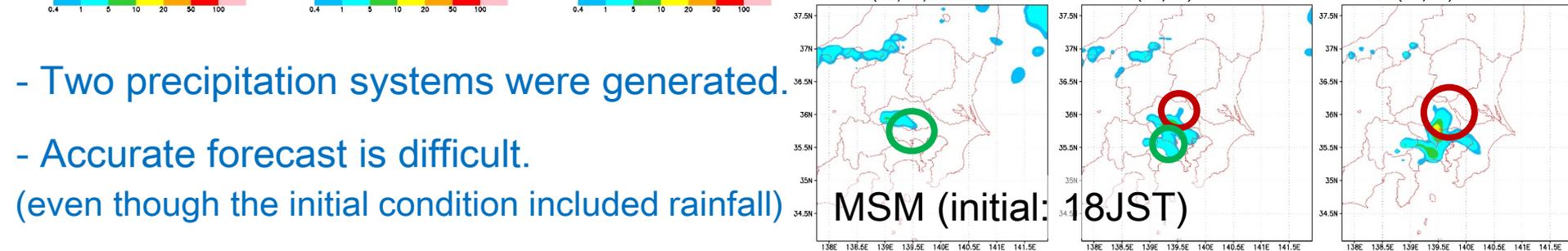
0.4 1 5 10 20 50 100

0.4 1 5 10 20 50 100

RAIN(mm/1hr) 201307181000

RAIN(mm/1hr) 201307181100

RAIN(mm/1hr) 201307181200



0.4 1 5 10 20 50 100

0.4 1 5 10 20 50 100

0.4 1 5 10 20 50 100

- Two precipitation systems were generated.
- Accurate forecast is difficult.  
(even though the initial condition included rainfall)

**Dense observations are expected to improve forecasts**

# Assimilated Dense Observations

Observation	Elements	Frequency	
Surface (JMA Surface observation and AMeDAS)	U, V, T	every 10 minutes	
GNSS	PWV	every 10 minutes	
Radar	Radial wind	every 10 minutes	Kashiwa, Haneda, Narita
Radiosonde	U, V, T, RH	every 3 hours	Tsukuba, Urawa, Yokosuka, Ryofu Maru

## Setting

Horizontal localization: **20 km**

Vertical localization: **0.1 lnP**

(PWV is not localized vertically)

Multiplicative inflation parameter: **1.2**

Observation error:

U, V: **1 m/s**

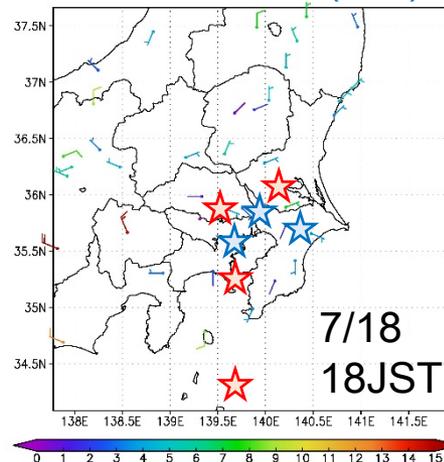
T: **1 K**

RH: **10%**

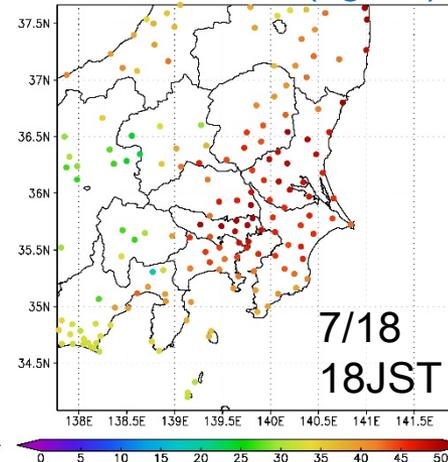
PWV: **5 kg/m<sup>2</sup>**

Radial wind: **3 m/s**

Surface wind (m/s)



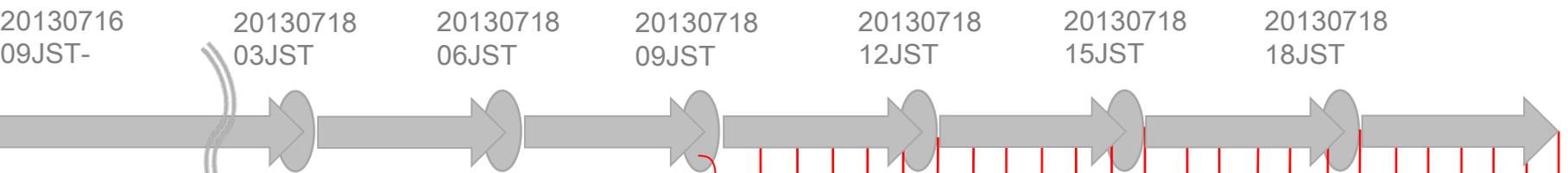
GNSS PWV (kg/m<sup>2</sup>)



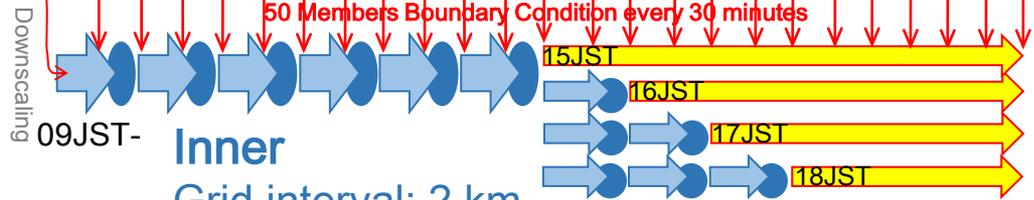
★:Radar  
★:Sonde

# Flow of Assimilation Experiments

Boundary condition: JMA GSM Forecast + Weekly Ensemble Perturbation



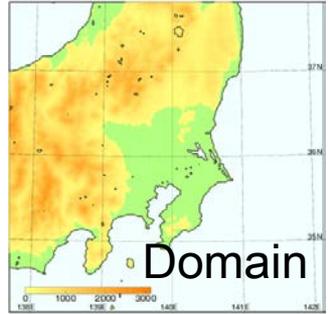
**Outer**  
 Grid interval: 10 km  
 Grid number: 361x289x50  
 Ensemble size: 50  
 Analysis window: 3 hour  
 (Operational Observations used in JMA Meso-DA every 30 minutes)



**Inner**  
 Grid interval: 2 km  
 Grid number: 200x200x60  
 Ensemble size: 50  
 Analysis window: 1 hour

**Extended Forecast**

➡ : Ensemble Forecasts  
 ● : Analysis (LETKF or EnVAR)

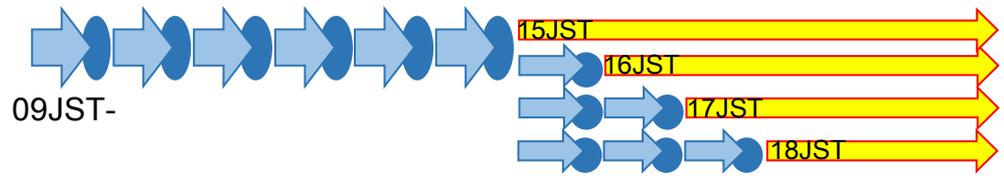


**Target:**  
 Local rain near Tokyo  
 in 20130718 **17-21JST**



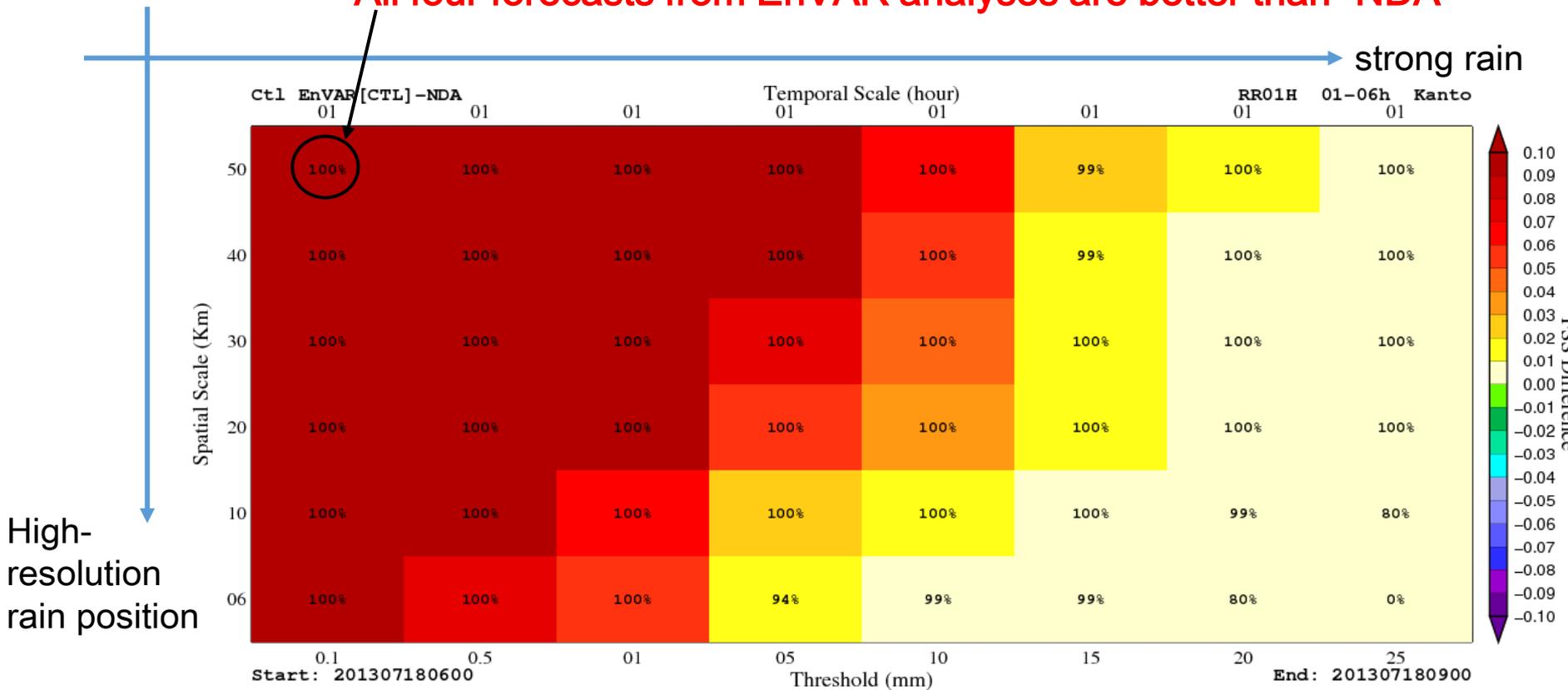
# Are Fractions Skill Scores improved?

$$FSS = 1 - \frac{[\sum_i (O_i - F_i)]^2}{[\sum_i O_i]^2 + [\sum_i F_i]^2}$$



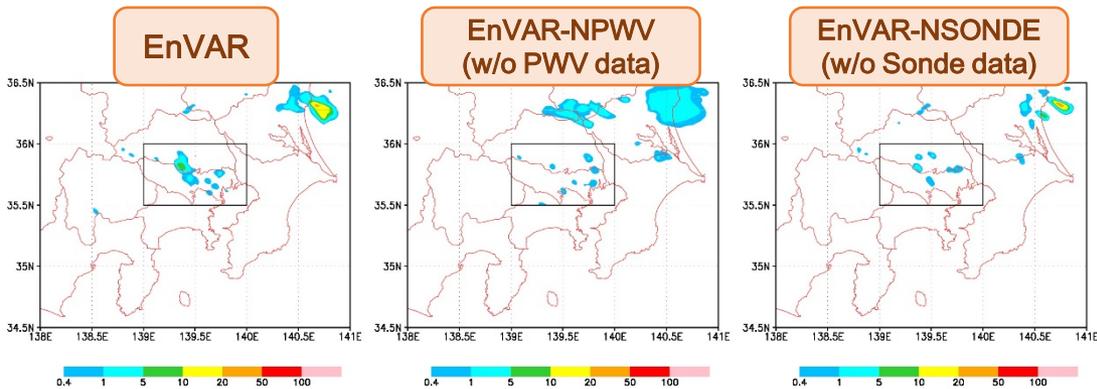
$O_i$  : number density of observed rainfall in i-th fraction  
 $F_i$  : number density of forecast rainfall in i-th fraction

**All four forecasts from EnVAR analyses are better than "NDA"**



# Impact of Dense Observations

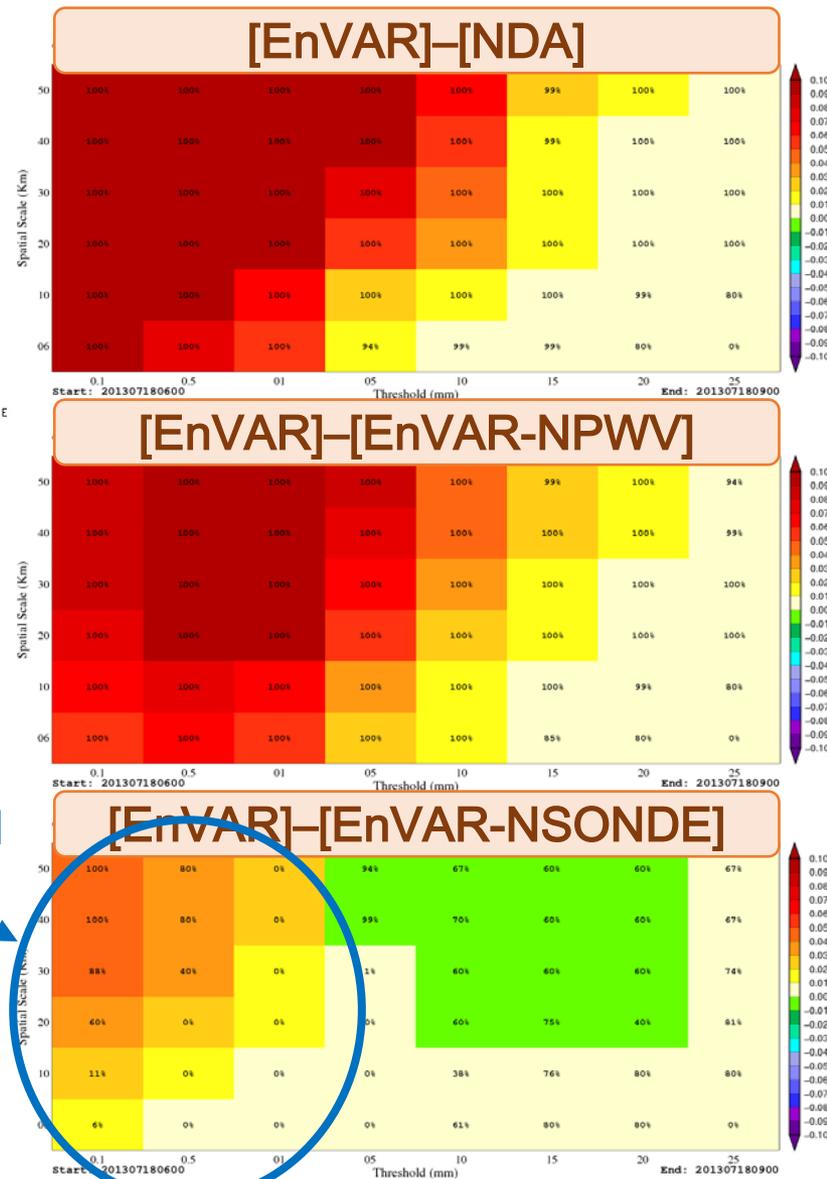
Rainfall in 18-19 JST



- PWV data greatly improved rainfall forecasts.

- Radiosonde data also improved weak rain forecasts.

**Both PWV and radiosonde data could improve rainfall forecasts**

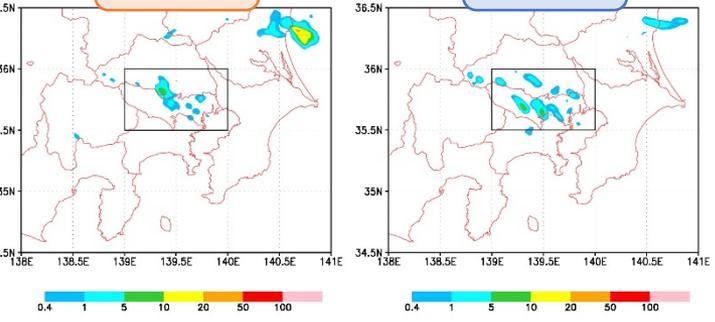


# EnVAR v.s. LETKF

Rainfall in 18-19 JST

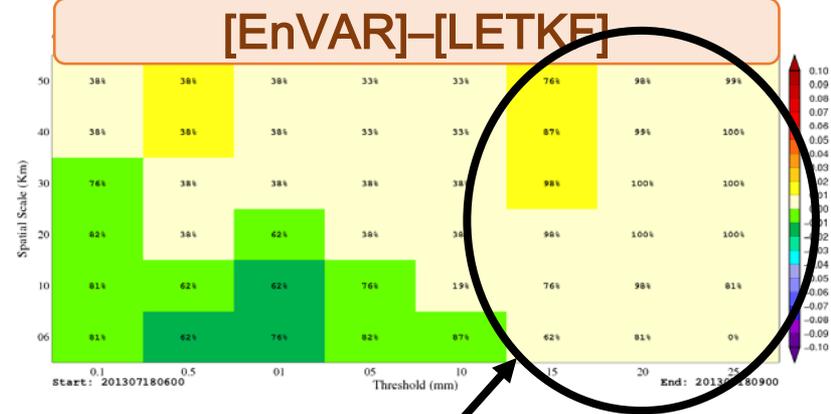
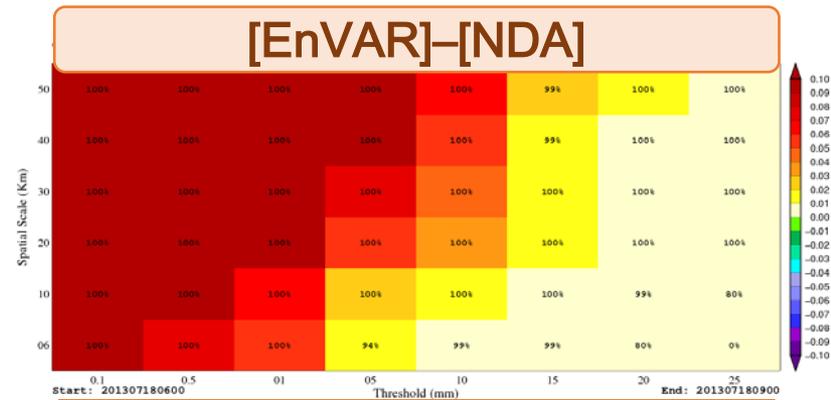
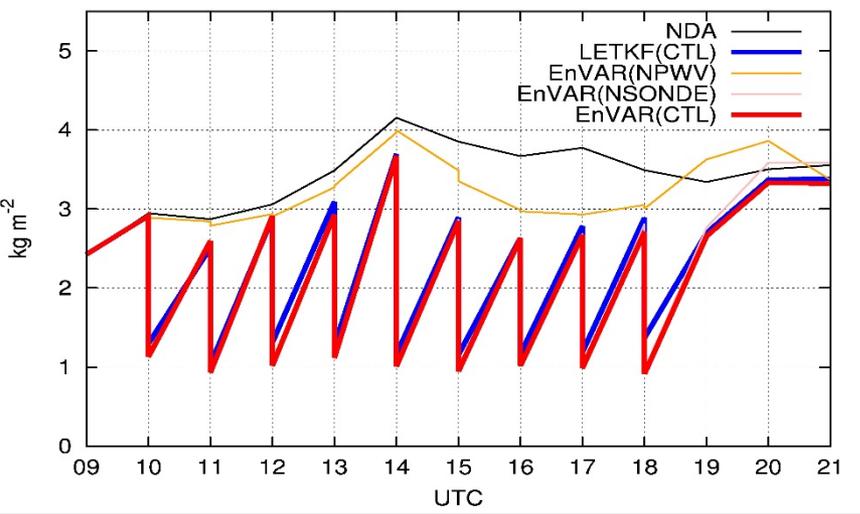
EnVAR

LETKF



- Difference between EnVAR and LETKF is small

Time series of RMS of (O-A) and (O-F) of PWV in the forecast-analysis cycles



In EnVAR, strong rainfall (> 15 mm/hr) forecasts are slightly better than that of LETKF

# Correlation between Rainfall and Initial States

## Correlation between $J$ and $x_n$

$$\text{CORR}(i, j) = \frac{\sum_m (J_m - \bar{J})(x_m(i, j) - \overline{x_m(i, j)})}{\sqrt{\sum_m (J_m - \bar{J})^2} \sqrt{\sum_m (x_m(i, j) - \overline{x_m(i, j)})^2}}$$

$i, j$  : grid number,  $m$ : ensemble member

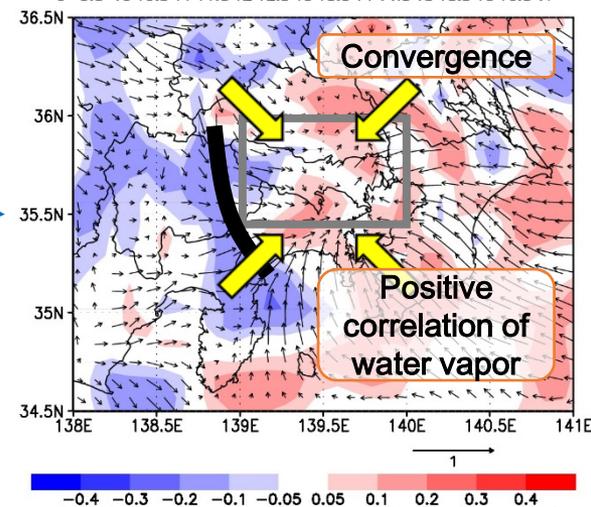
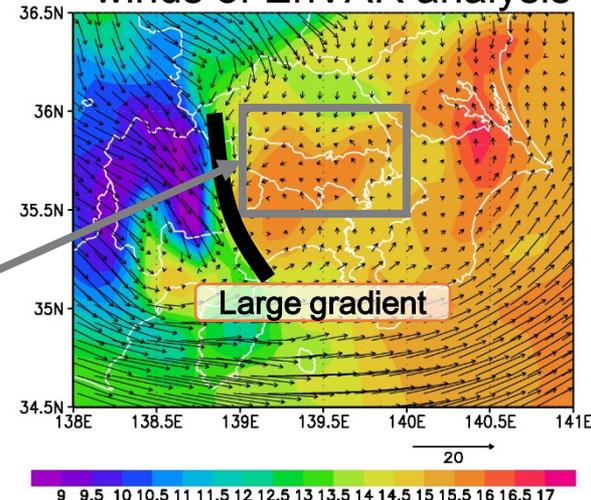
$J_m$  : 1-h rainfall (18–19JST) averaged in this area

$x_m(i, j)$  : variables in 0–1 km height at 18JST

If winds point to the direction of vectors in this figure, rainfall becomes stronger

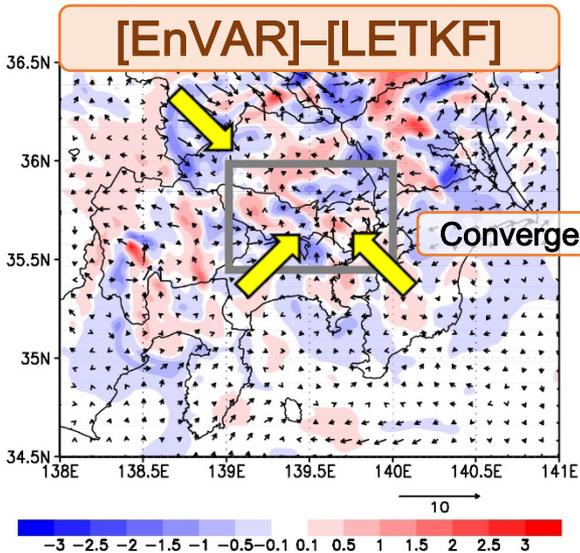
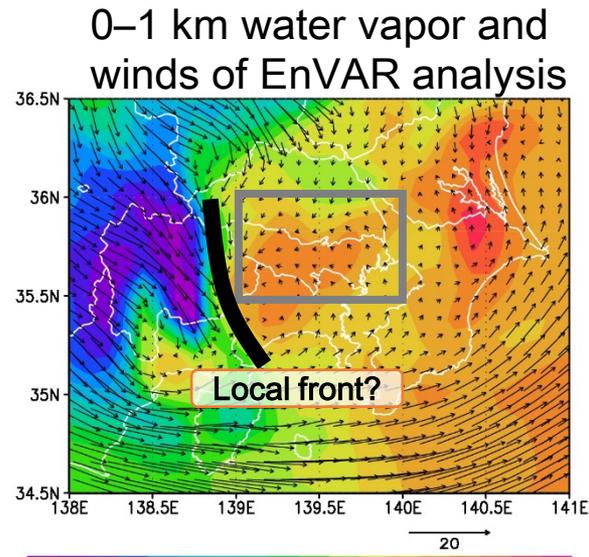
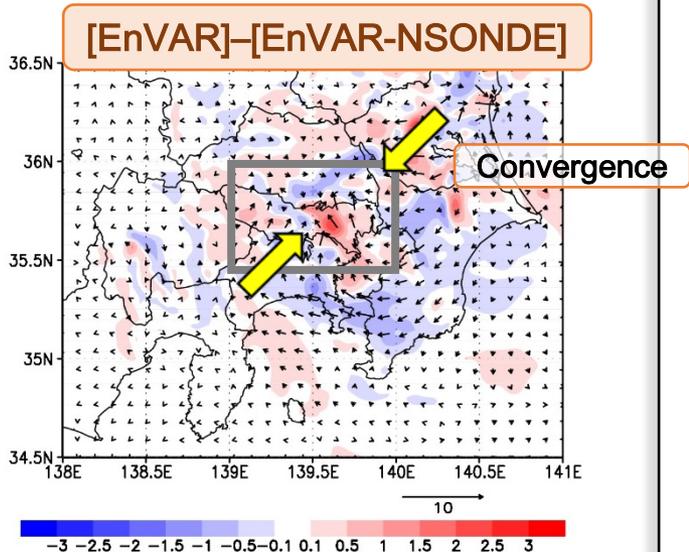
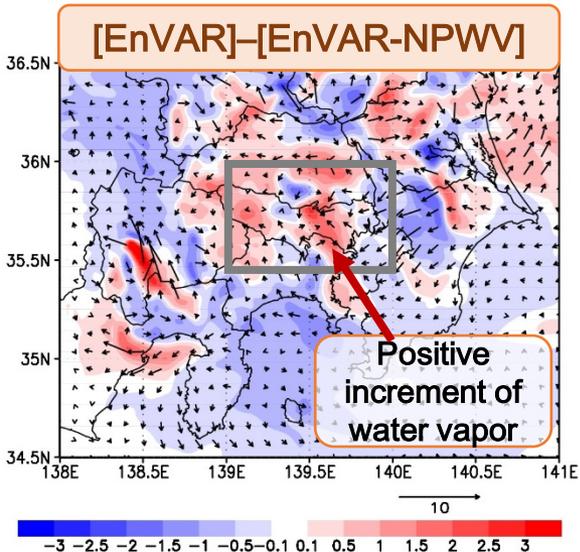
**Low-level convergence is correlated to rainfall intensity**

0–1 km water vapor and winds of EnVAR analysis



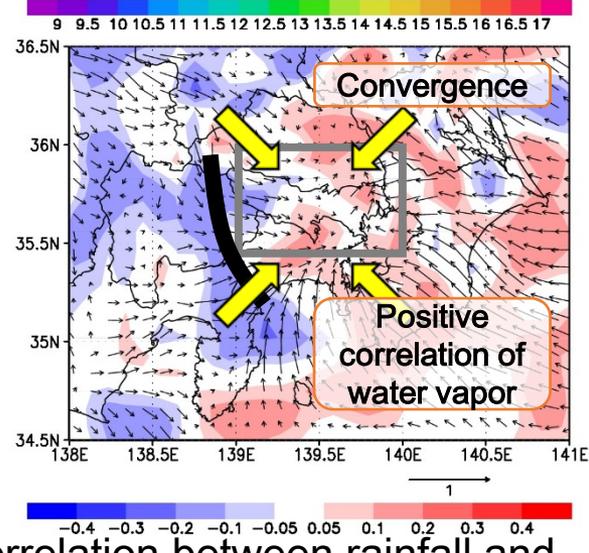
Correlation between rainfall and 0–1km water vapor and winds calculated by 51-member EnVAR

# Difference of Low-level variables



Difference of 0-1km water vapor and winds

**Increment of low-level water vapor and convergence makes rainfall stronger**



Correlation between rainfall and 0-1km water vapor and winds calculated by 51-member EnVAR

# Summary

We assimilated dense obs. for the local rainfall near Tokyo

- Impact of dense PWV and Radiosonde obs.
  - **PWV** improved rainfall forecast through correcting **low-level water vapor**
  - **Sonde obs.** improved rainfall forecast through correcting **low-level winds**
- Comparison between LETKF and EnVAR
  - **EnVAR** can make the analysis which is **closer to obs.** than LETKF.
  - Improvement of rainfall forecast by using EnVAR is small
- Correlation to rainfall based on ensemble forecasts
  - Low-level water vapor and convergence made local rainfall stronger

Are these impacts general? Verification in longer period requires.

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